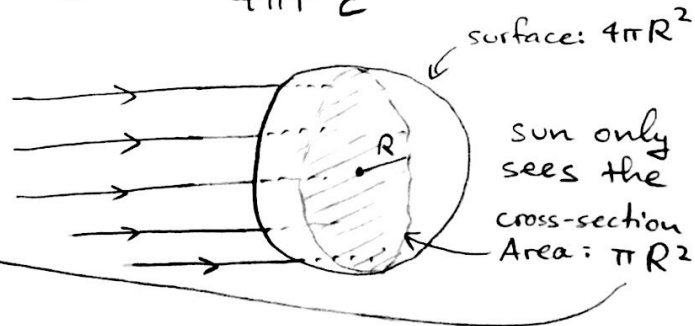


1. **Radiation Pressure** (YF 12th ed. 32.55). — Interplanetary space contains dust. Radiation pressure from the sun sets a lower limit on the size of such dust particles.
- (a) Write down F_G on a particle of mass m a distance r from the sun (mass M_\odot).
- (b) Let L be the luminosity of the sun, i.e. the rate at which it emits energy. Find the force exerted on the totally absorbing particle.
- (c) The mass density of a typical interplanetary dust particle is about 3000 kg/m^3 and the luminosity is $L = 3.9 \times 10^{26} \text{ W}$. Find the particle radius R such that the gravitational and radiation forces acting on the particle are equal in magnitude.

a)
$$F_G = \frac{GmM_\odot}{r^2}$$

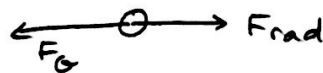
b) $F_{\text{rad}} = ?$; $P_{\text{rad}} = \frac{F_{\text{rad}}}{A} = \frac{I(r)}{c} = \frac{L}{4\pi r^2 c}$

$\Rightarrow F_{\text{rad}} = \frac{L\pi R^2}{4\pi r^2 c}$



c) At equilibrium,

$$F_G = F_{\text{rad}}$$



$$\frac{GmM_\odot}{r^2} = \frac{L\pi R^2}{4\pi r^2 c}$$

, where $m = \rho_m V = \rho_m \frac{4}{3}\pi R^3$

$$GM_\odot \frac{4}{3}\pi R^3 = \frac{L\pi R^2}{4\pi c}$$

$$R_0 = \frac{3L}{GM_\odot 16\pi c} = 0.19 \mu\text{m}$$

Since $F_G \propto R^3$, $F_{\text{rad}} \propto R^2$, the gravitational force dominates for $R > R_0$ (earth does not get blown away) and the radiation dominates for $R < R_0$ (no microdust)

2. **Photon.** A 100W lightbulb emits light at an average frequency of $f_m = 1\text{MHz}$. Calculate the number of photons per second passing through your pupil ($r = 0.5\text{cm}$) at a distance of 100m. How far would the lightbulb have to be for a flux of one photon per second?

$$a) \quad L = 100\text{ W} = \frac{N h f}{1\text{second}}$$

$$I = \frac{L}{4\pi r^2}$$

$$L_{\text{pupil}} = I \cdot A_{\text{pupil}} = \frac{L \pi R^2}{4\pi r^2} = \frac{n h f}{1\text{second}}$$

$$\Rightarrow \frac{n}{1s} = \frac{I A}{h f} = \frac{L R^2}{4 r^2 h f} = \frac{100 \cdot 25 \times 10^{-6}}{4 \cdot 100^2 \cdot 6.63 \times 10^{-34} \cdot 10^6} \frac{\text{photons}}{\text{seconds}}$$

$$= 0.9 \cdot 10^{20} \text{ photons/sec}$$

$$b) \quad \frac{n}{1s} = 1 = \frac{L R^2}{4 r^2 h f}$$

$$\Rightarrow r^2 = \frac{L R^2}{4 h f} = 0.9 \cdot 10^{24} \text{ m}^2$$

$$r = 9.5 \times 10^{11} \text{ m}$$

$$= 6 \text{ AU}$$

distance from sun to earth.