

## Discussion 7: Week 9

Table 7.1: Comparison of Angular Kinetics and Linear Kinetics

Linear Kinetics	Angular Kinetics
$x = x_0 + v_0t + at^2/2$	$\theta = \theta_0 + \omega_0t + \alpha t^2/2$
$v = dx/dt = v_0 + at$	$\omega = d\theta/dt = \omega_0 + \alpha t$
$a = dv/dt = d^2x/dt^2$	$\alpha = d\omega/dt = d^2\theta/dt^2$
$v_f^2 - v_i^2 = 2a(x_f - x_i)$	$\omega_f^2 - \omega_i^2 = 2\alpha(\theta_f - \theta_i)$
$m$	$I = \sum_i m_i r_i^2$
K.E. = $\frac{1}{2}mv^2$	K.E. = $\frac{1}{2}I\omega^2$

**Exercise 1** A computer disk drive is turned on starting from rest and has constant angular acceleration. If it took time  $t_2$  for the driver to make its first two complete revolutions, (a) how long did it take to make the first complete revolution, and (b) what is its angular acceleration?

**Exercise 2** A thin, uniform rod is bent into a square of side length  $a$ . If the total mass is  $M$ , find the moment of inertia about an axis through the center and perpendicular to the plane of the square. (Moment of inertia of a slender rod with axis through center is  $I = \frac{1}{12}ML^2$ )

**Exercise 3** In the system shown in the figure on the right, a mass  $m$  is released from rest and falls, causing the uniform cylinder of mass  $M$ , diameter  $R$  to turn about a frictionless axle through its center. How far will the mass have to descend to give the cylinder a kinetic energy of  $E$ ? (moment of inertia for a cylinder rotating about its center axis is given by  $I = \frac{1}{2}MR^2$ )

