

## Discussion 2: Week 3

**Exercise 1: Hypergravity** At its Ames Research Center, NASA uses its large 20-G centrifuge to test the effects of very large accelerations (hypergravity) on test pilots and astronauts. In this device, an arm of length  $L = 10$  m rotates about one end in a horizontal plane, and the astronaut is strapped in at the other end. Suppose that he is aligned along the arm with his head at the outermost end. The maximum sustained acceleration to which humans are subjected in this machine is  $a = 12.5g$ . (a) How fast must the astronaut's head be moving to experience this maximum acceleration? (b) What is the *difference* between the acceleration of his head and feet if the astronaut is 2.00 m tall? (c) How fast in rpm (rev/min) is the arm turning to produce the maximum sustained acceleration?

**Exercise 2:** Two tanks are engaged in a training exercise on level ground. The first tank fires a paint-filled training round with a muzzle speed of  $v_m$  at angle  $\theta$  above the horizontal while advancing toward the second tank with a speed of  $v_1$  relative to the ground. The second tank is retreating at  $v_2$  relative to the ground, but is hit by the shell. You can ignore air resistance and assume the shell hits at the same height above ground from which it was fired. Find the distance between the tanks

- (a) when the round was first fired and
- (b) at the time of impact.

**Exercise 3:** A projectile is fired from point  $A$  at an angle above the horizontal. At its highest point, after having traveled a horizontal distance  $D$  from its launch point, it suddenly explodes into two identical fragments that travel horizontally with equal but opposite velocities as measured *relative to the projectile just before it exploded*. If one fragment lands back at point  $A$ , how far from  $A$  (in terms of  $D$ ) does the other fragment land?

**Challenging Problem:** A projectile is thrown from a point  $P$ . It moves in such a way that its distance from  $P$  is always increasing. Find the maximum angle above the horizontal with which the projectile could have been thrown. You can ignore air resistance.